CamlP3I 1.0: User Manual

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Abstract

Writing parallel programs is not easy, and debugging them is usually a nightmare. To cope with these difficulties, a structured approach to parallel programs using skeletons and template based compiler techniques has been developed over the past years by several researchers, including the P3I group in Pisa.

This approach is based on the use of a set of predefined patterns for parallel computation which are really just functionals implemented via templates exploiting the underlying parallelism, so it is natural to ask whether marrying a real functional language like OCaml with the P3I skeletons can be the basis of a powerful parallel programming environment.

The CamlP3l prototype described in this document shows that this is the case. The prototype, written entirely in OCaml using a limited form of closure passing, allows a very simple and clean programming style, shows real speed-up over a network of workstations and as an added fundamental bonus allows logical debugging of a user parallel program in a sequential framework without changing the user code.

Chapter 1

Skeleton based programming and CamlP3I

In a skeleton based parallel programming model [6, 11, 9] a set of *skeletons*, i.e. of second order functionals modeling common parallelism exploitation patterns are provided to the user/programmer. The programmer uses skeletons to give parallel structure to an application and uses a plain sequential language to express the sequential portions of the parallel application. He/she has no other way to express parallel activities but skeletons: no explicit process creation, scheduling, termination, no communication primitives, no shared memory, no notion of being executing a program onto a parallel architecture at all.

CamlP3l is a programming environment that allows to write parallel programs in OCaml¹ according to a skeleton model derived by the one of P3l², provides seamless integration of parallel programming and functional programming and advanced features like sequential logical debugging (i.e. functional debugging of a parallel program via execution of the architecture at all parallel code onto a sequential machine) of parallel programs and strong typing, useful both in teaching parallel programming and in building of full-scale applications³.

In this chapter, we will first discuss the goals of our system design, then recall the basic notions of the skeleton model for structured parallel programming and describe the skeleton model provided by CamlP3I, providing an informal sequential (functional) and parallel semantics. It will be then time to describe how an CamlP3I program can be compiled and run on your system (Chapter 2). Then, we discuss more CamlP3I examples (Chapter 3) and detail CamlP3I implementation (Chapter 4) describing how we achieved our goals using to our advantage the flexibility of the OCaml system.

¹See http://pauillac.inria.fr/ocaml/

²See http://www.di.unipi.it/.susanna/p31.html

³See http://camlp31.inria.fr/ for relevant information, up to date references, documentation, examples, distribution code and dynamic web pages showcasing the CamlP3I features.

1.1 The system design goals

We started the development of the CamlP3I in 1998. At that time, the main goal of the project was to test the possibility to integrate parallel programming in a functional language using the skeleton model: after all, as we will see later, skeletons are just functions, so a functional language should provide the natural setting for them. We also wanted to preserve the elegance and flexibility of the functional model, and the strong type system that comes with OCaml. These goals were acheved in the first version of CamlP3I.

But during the implementation of the system, it turned out that we could get more than that: in our implementation, the sequential semantics that is traditionally used to describe the functional behaviour of the skeletons could actually be used to provide an elementary library allowing to execute the user code in a sequential mode, without modifying the user code. This is a major advantage of the approach: in our system, the user can easily debug the logic of his program running it with the sequential semantics on a sequential machine using all the traditional techniques (including tracing and step by step execution which are of no practical use on parallel systems), and when the program is logically correct he/she is guaranteed (assuming the runtime we provide is correct) to obtain a correct parallel execution. Although a similar approach has been taken in other skeleton based programming models, by using the OCaml programming environment this result happens to be particularly easy to achieve. This is definitely not the case of programs written using a sequential language and directly calling communication libraries/primitives such as the Unix socket interface or the MPI or PVM libraries, as the logic of the program is inextricably intermingled with low level information on data exchange and process handling.

Following this same idea (no changes to the user code, only different semantics for the very same skeletons), we also provided a "graphical semantics" that produces a picture of the process network used during the parallel execution of the user program.

Finally, we wanted a simple way to generate (from the user source code) the various executables to be run on the different nodes of a parallel machine: here the high level of abstraction provided by functional programming, coupled with the ability to send closures over a channel among copies of the same program provided the key to an elementary and robust runtime system that consists of a very limited number of lines of code.

But let's first of all introduce the skeleton model of CamIP3I 1.0.

1.2 The skeleton model of CamlP3I 1.0

A skeleton parallel programming model supports so-called 'structured parallel programming' [6, 11, 9]. Using such a model, the parallel structure/behaviour of any

application has to be expressed by using *skeletons* picked up out of a collection of predefined ones, possibly in a nested way. Each skeleton models a typical *pattern* of parallel computation (or *form* of parallelism) and it is parametric in the computation performed in parallel. As an example, pipeline and farm have been often included in skeleton collections. A *pipeline* just models the execution of a number of computations (stages) in cascade over a stream of input data items. Therefore, the pipeline skeleton models all those computations where a function $f_n(f_{n-1}(\dots(f_2(f_1(x)))\dots))$ has to be computed (the f_i being the functions computed in cascade). A *farm* models the execution of a given function in parallel over a stream of input data items. Therefore, farms model all those computations where a function f(x) has to be computed independently over n input data items in parallel.

In a skeleton model, a programmer must select the proper skeletons to program his/her application leaving all the implementation/optimization to the compiler/support. This means, for instance, that the programmer has no responsibility in deriving code for creating parallel processes, mapping and scheduling processes on target hardware, establishing communication frameworks (channels, shared memory locations, etc) or performing actual interprocess communications. All these activities, needed in order to implement the skeleton application code onto the target hardware are completely in charge to the compile/run time support of the skeleton programming environment. In some cases, the support also computes some parameters such as the parallelism degree or the communication grain needed to optimize the execution of the skeleton program onto the target hardware [19, 2, 20].

In the years, the skeleton model supplied by CamIP3I has evolved. Current CamIP3I version (1.0) supplies three kinds of skeletons:

- task parallel skeletons, modeling parallelism exploited between independent processing activities relative to different input data. In this set we have: pipe (cf. 1.3.4) and farm (cf. 1.3.3), whose semantics has already been informally described above. Such skeletons correspond to the usual task parallel skeletons appearing both in P3I and in other skeleton models [6, 11, 13].
- data parallel skeletons, modeling parallelism exploited computing different parts of the same input data. In this set, we provide mapvector (cf. 1.3.6) and reducevector (cf. 1.3.7). Such skeletons are not as powerful as the map and reduce skeletons of P3I. Instead, they closely resemble the map (*) and reduce (/) functionals of the Bird-Meertens formalism discussed in [3] and the map and fold skeletons in SCL [13]. The mapvector skeleton models the parallel application of a generic function f to all the items of a vector data structure, whereas the reducevector skeleton models a parallel computation folding all the elements of a vector with a commutative and associative binary operator \oplus).
- service or control skeletons, which are not parallel per se. Service skeletons are used to encapsulate OCaml non-parallel code to be used within other skeletons (see skeleton (cf. 1.3.2)), to iterate the execution of skeletons (loop skeleton

(cf. 1.3.5)), to transform a process network defined using skeletons in a valid OCaml function (parfun skeleton (cf. 1.3.8)) and to define global application structure (pardo skeleton (cf. 1.3.9)).

As an example, consider an application whose initial and final phase cannot be parallelized, while the behavior in the central part is clearly divided in two consecutive phases (stages) working on a stream of data. This can be modeled by the combination of CamlP3I skeletons in Fig. 1.1.

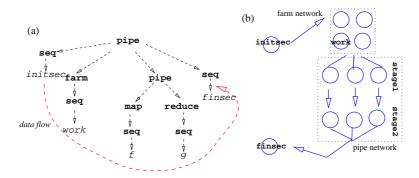


Figure 1.1: Structure of an example CamlP3I application: (a) the skeleton nesting, (b) processes participating to the implementation: pardo, stage1 and stage2.

All the structure is encapsulated in a pardo skeleton. initsec and finsec are two sequential OCaml functions describing the initial and final parts of application. The central part describes a parallel computation structured as a pipeline built out of two stages. If both stages are implemented via a sequential function (seq) data will flow as shown in Fig. 1.1.(a). In particular, the implementation spawns three processes: a 'pardo' process (executing the sequential parts) and a network of two processes implementing the pipeline (Fig. 1.1.(b)).

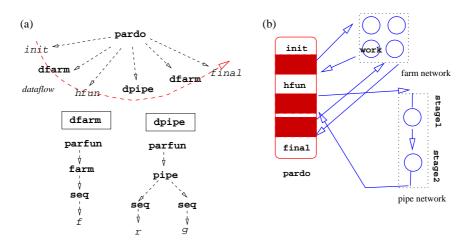


Figure 1.2: Further parallelizing the example CamlP3l application: (a) the skeleton nesting, (b) the processes participating to the implementation.

Now, suppose the programmer recognizes that the initsec is computationally intensive and can be decomposed in a sequential part (initsec) and a parallel part which applies a function work independently on each element on a stream of input data. In this case, we can use a farm skeleton to have a pool of replicas of work. Moreover, suppose the function stage1 boils down to applying a function f to all the elements of a vector and function stage2 "sums" up all the elements of the resulting vector by using an associative and commutative operator g. In this case, the programmer can refine the skeleton structure by using the combination in Fig. 1.2. Here, the four replicas of work act on different independent elements in the input stream, producing four stream of results (vectors) which are merged before entering the pipeline. Each stage is in turn implemented in parallel using four processes. In the first stage, each input vector is partitioned into four blocks. Each process takes care of applying f on one of the four blocks. Then in the second stage, each process sums up the elements in a block of the vector and then all the partial results are added before providing the final result back to the pardo (and to the finsec function).

The first "application outline" (Fig. 1.1) corresponds to the following (incomplete) CamlP3l code:

notice the use of seq skeleton to encapsulate ordinary OCaml functions and the use of parfun to define the pipe network. Here is the sketch of CamlP3l code for the second application outline (Fig. 1.2):

```
let degree = ref 4;
                                  (* parallel degree *)
let work _ x = ..;;
                                  (* to be farmed out *)
let f _ x = ...;;
                                  (* to be mapped *)
let g_{(x,y)} = ...;
                                   (* to be reduced *)
let pstage1 = mapvector(seq(f),!degree);;
let pstage2 = reducevector(seq(g),!degree);;
let pipe = parfun (fun () -> pstage1 || pstage2);;
let afarm = parfun (fun () -> farm (seq(farm_worker),!degree));;
pardo
  (fun () ->
     let y = pipe (afarm (initsec ())) in
       finsec y
  );;
```

here !degree refers to the number of parallel processes to be used in the skeleton implementation of mapvector, reducevector and farm. This value can vary in each execution of the application without recompiling (eg., using a configuration file). Details on how to write and run proper CamlP3I programs are given later in Chapter 2. In the current release, the user is supposed to explicitly give the number of processors to be used in each farm, mapvector and reduce skeleton. In other words the choice of the parallelism degree actually exploited in such skeletons is up to the programmer. It is foreseeable in a future release to ask the system to guess optimal values depending on available resources (following the approach of P3I [2, 19]), as it is discussed in more detail below.

Applications with a parallel structure given by skeletons (such as the ones outlined above) can be implemented by using *implementation templates* [6, 19]. An implementation template is a known, parametric way of exploiting the kind of parallelism modeled by a skeleton onto a particular target architecture. As an example, a template corresponding to the mapvector skeleton will take some input vector data, it will split the data into chunks holding one or more data items of the vector, schedule them to a set of "worker" processes computing the map function f and finally collect the results and rebuild the output vector data structure. All these operations will be performed by some processes, using either communications or shared memory locations for data communication. Such a template must, as its primary goal, implement in an efficient way the mapvector skeleton and therefore:

- it must implement any kind of map vector function f, and therefore must be parametric with respect to the input and output data types
- it must support any reasonable parallelism degree, therefore it must work (and provide effective parallelism exploitation) when executed on an arbitrary number of processors.

In CamlP3l 1.0, the parallelism degree of each skeleton is chosen by the programmer. In following releases, we will explore the possibility of using analytic performance models associated with the implementation template process networks to derive the parallelism degree automatically[21]. An analytic performance model is a set of functions computing different measures of the performance achieved by a template on the basis of a small set of machine dependent and user code parameters. Examples of machine dependent parameters are the cost of communication startup and the per-byte transmission cost. Examples of user code parameters are the mean and variance of execution time for user-defined sequential parts of the program and the size of data flowing between skeletons. The models describe the template behavior as a function of the resources used (e.g. the physical number of executors in a farm) and can be used by the skeleton support to predict such behavior and to tune resource allocation. A more detailed description of the whole automatic optimization process executed by a compiler using performance models for skeleton tuning is given in [19, 20, 21].

1.2.1 Parallel execution model

A parallel computation in CamIP3I is defined by three components:

- a set of plain sequential OCaml functions (CF, common functions in Figure 1.3),
- some clusters of parallel processes, each one defined by a suitable composition of skeleton combinators enclosed in a parfun (SF, skeleton functions in Figure 1.3) and
- a pardo application.

Each time a parfun(h) function definition is evaluated, a corresponding network of processes is created according to the skeleton composition in h. Each network transforms a stream of independent input data ... x_1, x_0 in a stream of output data ... $h(x_1), h(x_0)$ according to h.

When a pardo is evaluated, applications of common functions boil down to normal sequential evaluation, while applications of skeletal functions feed arguments data to the corresponding skeletal process network and are evaluated in parallel.

In practice, each pardo defines a network built out of all the processes in skeletal networks (parfun defined functions) plus a *root* process orchestrating all the computation. Both the root node and the generic nodes run in SPMD model. Initially, the root specializes all the generic nodes sending information on the actual process to be executed (eg., a farm dispatcher, a farm worker, a mapvector worker etc).

Then, the root process starts executing the pardo. If code is sequential, it is executed locally on the root node. Otherwise, if the evaluation of a parfun function is encountered, the root activates evaluation passing the relevant parameters to the corresponding network. The same network can be activated many times, each time an evaluation of the corresponding parfun function is encountered.

Notice that the execution model assumes an unlimited number of homogenous processors. In practical situations, processors will be less than processes and have heterogeneus capacity. The CamlP3I upport, possibly with some help from the programmer (using colors, see Sec. 1.4), is in charge of implementing this in a transparent way.

1.2.2 Discussion: a comparision with P3I

Even if CamlP3I skeletons are close to original P3I ones, the parallel evaluation model is completely different. Thus, for these familiar with P3I, it is interesting to highlight the main differences between two models and to give a brief account on the reasons that have lead to such a design change.

In the original P3I system (and, actually in initial versions of CamlP3I[10]), a program is clearly stratified into two levels: there is a skeleton *cap*, that can be composed of an arbitrary number of skeleton combinators, but as soon as one goes outside this cap, passing into the sequential code through the **seq** combinator, there is no way for the sequential code to call a skeleton. To say it briefly, the entry point

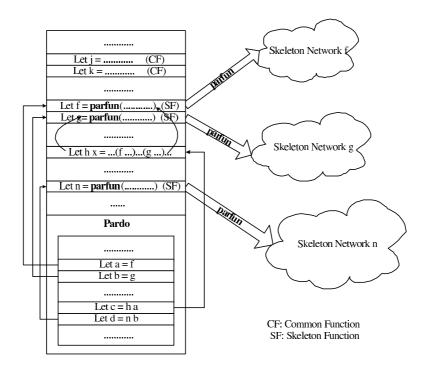


Figure 1.3: Parallel execution model: the role of parfun and pardo

of a P3I program *must* be a skeleton expression, and no skeleton expression is allowed anywhere else in the sequential code. Using current CamIP3I terminology, P3I restricts the pardo to contain one single call to a network defind with parfun, and without calls to sequential functions.

This restriction is quite reasonable when the goal is to build *a single* stream processing network described by the skeleton cap. However, it has several drawbacks in the general case:

- it breaks uniformity, since even if the skeletons *look like* ordinary functionals, they *cannot* be used as ordinary functions, in particular inside sequential code,
- many applications (such as the numerical algorithms described in [5]) boil down to simple nested loops, some of which can be easily parallelised, and some cannot; forcing the programmer to push all the parallelism in the skeleton cap could lead to rewriting the algorithm in a very unnatural way,
- indeed, a 'parallelizable' operation can be used at several stages in the algorithm: the P3I skeleton cap does not allow the user to specify that parts of the stream processing network can be shared among different phases of the computation, which is an essential requirement to avoid wasting computational resources.

To overcome all these difficulties and limitations, the 1.0 version of CamlP3I introduces the new parfun skeleton (not present in P3I), the very *dual* of the seq skeleton. In simple words, one can wrap a full skeleton expression inside a parfun,

```
(* computes x square *)
let farm_worker _ = fun x -> x *. x;;

(* prints a result *)
let print_result x = print_float x; print_newline();;

let compute = parfun (fun () -> (farm (seq(farm_worker),4)));;

pardo(fun () ->
    let is = P3lstream.of_list [1.0;2.0;3.0;4.0;5.0;6.0;7.0;8.0] in
    let s' = compute is in P3lstream.iter print_result s';
);;
```

Figure 1.4: CamIP3I code using a farm to square a stream of float.

and obtain a regular OCaml stream processing function, usable with no limitations in any sequential piece of code: a parfun encapsulated skeleton behaves exactly as a normal function that receives a stream as input, and returns a stream as output. However, in the parallel semantics, the parfun combinator gets a parallel interpretation, so that the encapsulated function is actually implemented as a parallel network (the network to which the parfun combinator provides an interface). Since many parfun expressions may occur in an CamlP3l program, there may be several disjoint parallel processing networks at runtime. This implies that, to contrast with P3l, the CamlP3l model of computation requiers a main sequential program (the pardo): this main program is responsible for information interchange with the various parfun encapsulated networks.

1.2.3 A simple example: farming square computation

It is now time to discuss a simple but complete CamlP3I program. The program in Figure 1.4 uses a farm to compute a very simple function over a stream of floats. First we have two standard OCaml functions: farm_worker which simply computes the square of a float argument and print_result which dumps results on the stardard output. Notice that farm_worker takes two parameters instead of one as it would seem reasonable. The extra parameter (_) is required by the seq skeleton type and is used in general to provide local initialization data (for instance, an initialization matrix, some initial seed or the like). In this simple case, initialization data are not needed and the parameter is just ignored by farm_worker. This optional initialization is provided for all CamlP3I skeletons (see Section 1.3.1). Function compute uses parfun to define a parallel network built by a single farm, in particular:

```
seq(farm_worker)
```

turns the sequential farm_worker function into a 'stream processor' applying it to a stream of input values. Then, an instance of the farm skeleton is defined with

```
farm (seq(farm_worker),4)
```

which spawns four workers. Finally,

```
parfun (fun () -> (farm (seg(farm_worker),4)));;
```

encapsulates the skeleton network into a standard OCaml function.

The last pardo defines how sequential functions and parallel modules are interconnected. In this case, we have a single parallel module (compute) and two sequential parts. The first sequential part builds up the data stream (using the standard CamlP3I library function

```
P3lstream.of_list [1.0;2.0;3.0;4.0;5.0;6.0;7.0;8.0]
```

which turns lists in streams) and the second part applies print_results to all the elements in the stream (using standard stream iterator P3lstream.iter). The global network is shown in Figure 1.5, where arrows point out the data flow among processes.

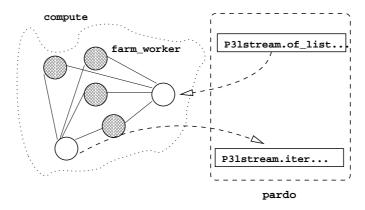


Figure 1.5: Overall process network of the simple farm squaring a stream of double.

1.3 Skeleton syntax, semantics, and types

Here we describe the syntax, the informal semantics, and the types assigned to each skeleton combinator.

Each skeleton is a stream processor, transforming an input stream into an output stream and is equipped with three semantics:

sequential semantics a suitable sequential OCaml function transforming all the elements of the input stream;

parallel semantics a process network implementing the stream transformation in parallel;

graphical semantics a graphical representation of the process network corresponding to the parallel semantics.

1.3.1 On the type of skeleton combinators

First of all, let's explain why the actual OCaml types of our skeleton combinators are a bit more complex than those used by other skeleton systems (eg., [13]). In effect, our types seem somewhat polluted by spurious additional unit types, compared to the types one would expect.

For istance, consider the seq combinator. As informally discussed above, seq encapsulates any OCaml function f into a sequential process which applies f to all the inputs received in the input stream. This means that, writing seq f, any OCaml function with type f: 'a -> 'b is wrapped into a sequential process (this is reminiscent to the lift combinator used in many stream processing libraries of functional programming languages).

```
Hence, a strightforward type for seq would be
('a -> 'b) -> 'a stream -> 'b stream.

However, in CamlP3I, seq is declared as
seq : (unit -> 'a -> 'b) -> unit -> 'a stream -> 'b stream
```

meaning that the lifted function argument f gets an extra unit argument. In effect, in real-world application, the user functions may need to hold a sizeable amount of local data (e.g. some huge matrices that have to be initialised in a numerical application), and we decided to have a type general enough to allow the user to finely describe where and when those data have to be initialized and/or copied.

Reminiscent to partial evaluation and λ -lifting, we reuse the classical techniques of functional programming to initialize or allocate data globally and/or locally to a function closure. This is just a bit complicated here, due to the higher-order nature of the skeleton algebra, that in turn reflects the inherent complexity of parallel computing:

• global initialization: the data is initialised once and for all, and is then replicated in every copy of the stream processor that a farm, a mapvector or a reducevector may launch; this was already available in the previous versions of CamlP3I, since we could write

```
let f =
  let localdata = do_huge_initialisation_step () in
  fun x -> compute (localdata, x);;
...
farm (seq f, 10)
```

• *local initialization*: the data is initialised by each stream processor, *after* the copy has been performed by a farm or a mapvector skeleton; this was just impossible in the previous versions of CamlP3I; with unit types, it is now easy to achieve:

```
let f() =
```

```
let localdata = do_huge_initialisation_step () in
  fun x -> compute (localdata, x);;
...
farm (seq f, 10)
```

when the farm skeleton creates 10 copies of seq f, each copy is created by passing () to the seq combinator, which in turn passes () to f, producing the allocation of a different copy of *localdata* for each instance⁴.

Note also that the old behaviour, namely CamlP3l version 1.0, where a unique initialization was shared by all copies, is still easy (and can be freely combined to further local initializations if needed):

```
let f =
  let localdata = do_huge_initialisation_step () in
  fun () -> fun x -> compute (localdata, x);;
...
farm (seq f, 10)
```

To sum up, the extra unit parameters give the programmer the hability to decide whether local initialisation data in his functions are shared among all copies or not. In other words, we can regard the skeleton combinators in the current version of CamlP3I as "delayed skeletons", or "skeleton factories", that produce an instance of a skeleton every time they are passed an () argument.

In the following sections we detail the types and semantics of all the skeletons and provide some usage examples.

1.3.2 The seq skeleton

The seq skeleton encapsulates an OCaml function f into a stream process which applies f to all the inputs received on the input stream and sends off the reselts on the output stream. Any OCaml function with type

```
f: unit -> 'a -> 'b
```

can be encapsulated in the seq skeletons as follows:

```
seq f
```

The central point is that the function must be *unary*, i.e. functions working on more that one argument must collect them in a single tuple before being used in a seq. For instance, the fragment

```
let g _ (x,y) = x *. y;;
let redmul = parfun (fun () -> reducevector(seq(g),6));;
```

shows how to encapsulate a float binary operator (*.) to use it within a reducevector with 6 working processes.

⁴In practice, the initialization step may do weird, non referentially transparent things, like opening file descriptors or negociating a network connection to other services: it is then crucial to allow the different instances of the user's function to have their own local descriptors or local connections to simply avoid the chaos.

1.3.3 The farm skeleton

The farm skeleton computes in parallel a function f over different data items appearing in its input stream.

From a functional viewpoint, given a stream of data items x_1, \ldots, x_n , and a function f, the expression farm(f, k) computes $f(x_1), \ldots, f(x_n)$. Parallelism is gained by having k independent processes that compute f on different items of the input stream.

If f has type (unit -> 'b stream -> 'c stream), and k has type int, then farm(f,k) has type unit -> 'b stream -> 'c stream. In terms of (parallel) processes, a sequence of data appearing onto the input stream of a farm is submitted to a set of worker processes. Each worker applies the same function (f, which can be in turn difined using parallel skeletons) to the data items received and delivers the result onto the output stream. The resulting process network looks like the following:

where the emitter process takes care of task-to-worker scheduling (possibly taking into account some load balancing strategy).

The farm function takes two parameters:

- the first denoting the skeleton expression representing the farm worker computation,
- the second denoting the parallelism degree the user decided for the farm, i.e. the number of worker processes that have to be set up in the farm implementation.

Figure 1.6 shows an CamlP3l program which chooses randomly a number from a list and writes it to the file magic_number. Notice the local initialization of the random number generator (which takes a different seed in each worker) and the local open of the file to be written. In Figure 1.7 you can see how the worker code can be simply transformed to have all the workers share the same filed descripto if needed (global initialization).

1.3.4 The pipeline skeleton

The pipeline skeleton is denoted by the infix operator |||; it performs in parallel the computations relative to different stages of a function composition over different

Figure 1.6: A simple farm example (with local initialization)

Figure 1.7: Worker code using global initialization to share file descriptor

data items of the input stream.

Functionally, $f_1 | | | | f_2 ... | | | | f_n$ computes $f_n (... f_2 (f_1(x_i)) ...)$ over all the data items x_i in the input stream. Parallelism is now gained by having n independent parallel processes. Each process computes a function f_i over the data items produced by the process computing f_{i-1} and delivers its results to the process computing f_{i+1} .

```
If f_1 has type (unit -> 'a stream -> 'b stream), and f_2 has type (unit -> 'b stream -> 'c stream), then f_1|||f_2| has type unit -> 'a stream -> 'c stream.
```

In terms of (parallel) processes, a sequence of data appearing onto the input stream of a pipe is submitted to the first pipeline stage. This stage computes the function f_1 onto every data item appearing onto the input stream. Each output data item computed by the stage is submitted to the second stage, computing the function f_2 and so on and so on until the output of the n-1 stage is submitted to the last stage. Eventually, the last stage delivers its own output onto the pipeline output channel. The resulting process network looks like the following:

For instance, a pipeline made out of three stages, the first one squaring integers, the second one multiplying integers by 2 and the third one incrementing integers can be written as follows:

```
let square _ x = x * x;;
let double _ x = 2 * x;;
let inc _ x = x + 1;;
let apipe = parfun (fun () -> seq(square) ||| seq(double) ||| seq(inc));;
```

A pipeline models (parallel) function composition, thus input and output types of stages should match. This means that if stage (i-1) has type unit -> 'c -> 'a stage (i+1) has type unit -> 'b -> 'd stage i-th must have type unit -> 'a -> 'b.

1.3.5 The loop skeleton

The loop skeleton named loop; it computes a function f over all the elements of its input stream until a boolean condition g is verified. A loop has type

```
('a -> bool) * (unit -> 'a stream -> 'a stream)
```

provided that f has type unit -> 'a stream -> 'a stream and g has type 'a -> bool. Function f is computed before testing termination, thus it is applied at least one time to each input stream element. In terms of (parallel) processes, a sequence of data appearing onto the input stream of a loop is submitted to a loop in stage. This stage just merges data coming from the input channel and from the feedback channel and delivers them to the loop body stage. The loop body stage computes f and delivers results to the loop end stage. This latter stage computes g and either delivers (f x) onto the output channel (in

case (g (f x)) turns out to be true) or it delivers the value to the loop in process along the feedback channel ((g (f x)) = false). The resulting process network looks like the following:

For instance, the following loop increments all the integer data items in the input stream until they become divisible by 5:

```
let notdivbyfive x = (x mod 5 <> 0);;
let inc _ x = x + 1;;
let aloop = parfun (fun () -> loop(notdivbyfive,seq(inc)));;
```

The output of this function on the sequence

```
3,7,10,14
```

is 5,10,15,15. In particular, the call theloop 10 returns 15 as the body seq(inc) is evaluated on input data *before* the condition, and therefore the first time the condition is evaluated on 11 and not on 10.

1.3.6 The map skeleton

The map skeleton is named mapvector; it computes in parallel a function over all the data items of a vector, generating the (new) vector of the results.

Therefore, for each vector X in the input data stream, mapvector(f, n) computes the function f over all the items of $X = [x_1, \ldots, x_n]$, using n distinct parallel processes that compute f over distinct vector items $([f(x_1), \ldots, f(x_n)])$.

If f has type (unit -> 'a stream -> 'b stream), and n has type int, then mapvector(f, n) has type unit -> 'a array stream -> 'b array stream.

In terms of (parallel) processes, a vector appearing onto the input stream of a map vector is split n elements and each element is computed by one of the n workers. Workers apply f to the elements they receive. A collector process is in charge of gluing together all the results in a single result vector.

Different strategies can be used to distribute a vector [|x1;...;xm|] appearing in the input data stream to the workers. As an example the emitter:

- may round robin each xi to the workers ($\{w1, ... wn\}$). The workers in this case simply compute the function $f:'a \to 'b$ over all the elements appearing onto their input stream (channel).
- may split the input data vector in exactly n sub-vectors to be delivered one to each one of the worker processes. The workers in this case compute an Array.map f over all the elements appearing onto their input stream (channel).

Summarizing, the emitter process takes care of (sub)task-to-worker scheduling (possibly implementing some kind of load balancing policy), while the collector process takes care of rebuilding the vector with the output data items and of delivering the new vector onto the output data stream. mapvector takes two arguments:

- the skeleton expression denoting the function to be applied to all the vector elements,
- the parallelism degree of the skeleton, i.e. the number of processes to be used in the implementation.

For instance, the following code works on a stream of integer vectors and squares each vector element. The skeleton has a parallelism degree of 10, that is ten parallel processes are used to compute each vector in the stream.

```
let square _ x = x * x;;
let amap = parfun (fun () -> mapvector(seq(square),10));;
the result on a single array is as follows
# amap [|1;2;3;4;5|];;
- : int array = [|1; 4; 9; 16; 25|]
```

1.3.7 The reduce skeleton

The reduce skeleton is named **reducevector**; it folds a function over all the data items of a vector.

Therefore, $reducevector(\oplus, n)$ computes $x_1 \oplus x_2 \oplus \ldots \oplus x_n$ out of the vector x_1, \ldots, x_n , for each vector in the input data stream. The computation is performed using n different parallel processes that compute f.

If \oplus has type (unit -> 'a * 'a stream -> 'a stream), and n has type int, then $reducevector(\oplus, n)$ has type unit -> 'a array stream -> 'a stream.

In terms of (parallel) processes, a vector appearing onto the input stream of a reducevector is processed by a logical tree of processes. Each process is able to compute the binary operator g. The resulting process network looks like the following tree:

In this case, the emitter process is the one delivering either couples of input vector data items or couples of sub-vectors of the input vector to the processes belonging to the tree base. In the former case, $\log(n)$ levels of processes are needed in the tree, in the latter one, any number of process levels can be used, and the number of sub-vectors to be produced by the emitter can be devised consequently.

The reducevector function takes two parameters as usual:

- the first parameter is the skeleton expression denoting the binary, associative and commutative operation (these properties must be ensured by the programmer to have a correct execution)
- the second is the parallelism degree, i.e. the number of parallel processes that have to be set up to execute the reducevector computation.

For instance, the following skeleton instance accepts in input a stream of vectors and, for each vector, computes the sum of all elements using the arithmetic + operator.

```
let areduce = parfun
  (fun () -> reducevector(seq(fun _ (x,y) -> x + y),10));;
the result on a single array is as follows
# areduce [|1;2;3;4|];;
- : int = 10
```

1.3.8 The parfun skeleton

One would expect parfun to have type (unit -> 'a stream -> 'b stream) -> 'a stream -> 'b stream' -> 'b stream', parfun returns a stream processing function of type 'a stream -> 'b stream.

parfun's actual type introduces an extra level of functionality: the argument is no more a skeleton expression but a functional that returns a skeleton:

```
val parfum :
  (unit -> unit -> 'a stream -> 'b stream) -> 'a stream -> 'b stream
```

This is necessary to guarantee that the skeleton wrapped in a parfun expression will only be launched and instanciated by the main program (pardo), not by any of the multiple running copies of the SPMD binary, even though thoses copies may evaluate the parfun skeletons; the main program will actually create the needed skeletons by applying its functional argument, while the generic copies will just throw the functional away, carefully avoiding to instanciate the skeletons.

1.3.9 The pardo skeleton: a parallel scope delimiter

Typing

Finally, the pardo combinator defines the scope of the expressions that may use the parfun encapsulated expressions.

```
val pardo : (unit -> 'a) -> 'a
```

pardo takes a thunk as argument, and gives back the result of its evaluation. As for the parfun combinator, this extra delay is necessary to ensure that the initialization of the code will take place exclusively in the main program and not in the generic SPMD copies that participate to the parallel computation.

Parallel scoping rule

In order to have the parfun and pardo work correctly together the following scoping rule has to be sollowed:

- functions defined via the parfun combinator must be defined before the occurrence of the pardo combinator,
- those parfun defined functions can only be *executed within* the body of the functional parameter of the pardo combinator,
- no parfun can be used directly inside a pardo combinator.

Structure of an CamlP3l program

Due to the scoping rule in the pardo, the general structure of an CamlP3l program looks like the following:

```
(* (1) Functions defined using parfun *)
let f = parfun(skeleton expression)
let g = parfun(skeleton expression)
(* (2) code referencing these functions under abstractions *)
let h x = \dots (f \dots) \dots (g \dots) \dots
(* NO evaluation of code containing a parfun is allowed outside pardo *)
(* (3) The pardo occurrence where parfun encapsulated
       functions can be called. *)
pardo
 (fun () ->
    (* NO parfun combinators allowed here *)
    (* code evaluating parfun defined functions *)
    . . .
    let a = f ...
    let b = h \dots
)
(* finalization of sequential code here *)
```

At run time, in the sequential model, each generic copy just waits for instructions from the main node; the main node first evaluates the arguments of the parfun combinators to build a representation of the needed skeletons; then, upon encountering the pardo combinator, the main node initializes all the parallel computation networks, specialising the generic copies (as described in details in [10]), connects these networks to the sequential interfaces defined in the parfun's, and then runs the sequential code in its scope by applying its function parameter to ():unit. The whole picture is illustrated in Figure 1.3. The skeleton networks are initiated only once but could be invoked many times during the execution of pardo.

1.4 Load balancing: the colors

In the CamlP3I system, the combinators expressions govern the shape of the process network and the execution model assumes a 'virtual' processor, for each process. The mapping of virtual to physical processors is delegated to the CamlP3I system. The mapping is currently not optimized in the system. However, programs and machines can be annotated by the programmer using *colors*, which can pilote the virtual-to-physical mapping process.

The idea is to have the programmer to rank the relative 'weight' of skeleton instances and the machine power in a range of integer values (the colors). Then, weights are used to generate a mapping in which load is evenly balanced on the partecipating machine according to their relative power.

Pushing the difficult part of the generaion of weights to the programmer's knowledge and ability, this simple and practical idea gives surprisingly good results in practice.

Let's consider as an example, the skeletal expression we discussed in the example (Sec 1.2.3):

farm (seq
$$(fun \ x \rightarrow x * x), 16)$$

that corresponds to a network of one emitter node, one collector node, and 16 worker nodes which compute the square function. There are numerous ways of mapping a set of virtual nodes to a set of physical nodes.

If no information is provided, the support uses a simple round robin, which maps virtual to physical nodes in a cyclic way: first all phisical processors get one process then we start again from the beginning until virtual processors are all allocated. Unfortunately, such a solution doesn't take into account the load balancing constraints: all the physical (resp. virtual) nodes are considered equivalent in computing power and are used evenly.

If the programmer knows more about machines and processes he/she can tell the system using colors. A color is an optional integer parameter that is added to CamlP3l expressions in the source program and to the execution command line of the compiled program. We use the regular OCaml's optional parameters syntax, with keyword col, to specify the colors of a network of virtual nodes. For example, writing farm ~col:k~(f, n) means that all virtual nodes inside this farm structure should be mapped to some physical nodes with a capability ranking k. The scope of a color specification covers all the inner nodes of the structure it qualifies: unless explicitly specified, the color of an inside expression is simply inherited from the outer layer (the outermost layer has a default color value of 0 which means no special request).

For combinators farm, mapvector and reducevector, in addition to the color of the combinator itself, their is an additional optional color parameter colv. A colv[] specification is a color list (i.e. an int list) that specifies the colors of the parallel worker structures that are arguments of the combinator. As an example, the CamlP3I expression

```
map ~col:2 ~colv:[ 3; 4; 5; 6 ] (seq f, 4)
```

is a mapvector skeleton expression, with emitter and collector nodes of rank 2, and four worker nodes (four copies of seq f) whith respective ranks 3, 4, 5, and 6.

To carefully map virtual nodes to physical nodes, we also need a way to define the colors of physical nodes. This information is specified on the command line when launching the program (see Section 2). One can write:

where ip_i:port_i#color_i indicates the ip address (or name), the port, and the color of the physical node i participating to the computation. The port and color here are both optional. With no specified port, a default p3lport is used; with no color specification, the default color 0 is assumed.

If the colors of all the virtual processors and all the physical processors have a one-to-one correspondance, the mapping is easy. But such a perfect mapping does not exist in general: first of all, there is not always equality between the amount of physical processors we have and the amount of virtual processors we need; second, in some very complex CamlP3I expressions, it is complex and boring for the programmer to calculate manually how many virtual nodes are needed for each color class.

So, we decided to use a simple but flexible mapping algorithm, based on the idea that what a color means is not the exact capability required but the lowest capability acceptable. For example, a virtual node with color value 5 means a physical node of color 5 is needed, but if there is no physical node with value 5, and there exists a physical node of color 6 free and available, why don't we take it instead? In practice, we sort the virtual nodes in decreasing order of their color values, to reflect their priority in choosing a physical node: virtual nodes with bigger colors should have more privilege and choose their physical node before the nodes with smaller colors. Then, for each virtual node, we lists all the physical nodes with a color greater than or equal to the virtual node color. Among all those qualified ones, the algorithm finally associates the virtual node with the qualified node which has the smallest work load (the one that has the least number of virtual nodes that have been assigned to it).

This algorithm provides a mapping process with some degree of automatization and some degree of manual tuning, but one has to keep in mind that the *color* designs a computational class, qualitatively, and is not an exact quantitative estimation of the computational power of the machine, as the current version of CamlP3I does not provide yet the necessary infrastructure to perform an optimal mapping based on precise quantitative estimations of the cost of each sequential function and the capabilities of the physical nodes, so that we cannot guarantee our color-based mapping algorithm to be highly accurate or highly effective.

Still, the "color" approach is accurate and simple enough to be quite significant to the programmer: according to the experiments we have conducted, it indeed achieved some satisfactory results in our test bed case (see [5]).

Figure 1.8 summarizes the types of the combinators, exactly as they are currently available to the programmer in the 1.0 version of CamlP3I, including the optional color parameters.

```
type color = int
val seq :
  ?col:color ->
  (unit -> 'a -> 'b) -> unit -> 'a stream -> 'b stream
val ( ||| ) :
  (unit -> 'a stream -> 'b stream) ->
  (unit -> 'b stream -> 'c stream) -> unit -> 'a stream -> 'c stream
val loop :
  ?col:color ->
  ('a -> bool) * (unit -> 'a stream -> 'a stream) ->
  unit -> 'a stream -> 'a stream
val farm :
  ?col:color ->
  ?colv:color list ->
  (unit -> 'b stream -> 'c stream) * int ->
  unit -> 'b stream -> 'c stream
val mapvector :
  ?col: color ->
  ?colv:color list ->
  (unit -> 'b stream -> 'c stream) * int ->
  unit -> 'b array stream -> 'c array stream
val reducevector :
  ?col:color ->
  ?colv:color list ->
  (unit -> ('b * 'b) stream -> 'b stream) * int ->
  unit -> 'b array stream -> 'b stream
val parfun :
  (unit -> unit -> 'a stream -> 'b stream) -> 'a stream -> 'b stream
val pardo : (unit -> 'a) -> 'a
```

Figure 1.8: The (complete) types of the CamIP3I skeleton combinators

Chapter 2

Running your CamlP3l program

We give here a practical tutorial on how to use the system, without entering into the implementation details of the current version of CamIP3I.

As mentioned above, once you have written an CamlP3I program, you have several choices for its execution, since you can without touching your source:

sequential run your program sequentially on one machine, to test the logic of the algorithm you implemented with all the usual sequential debugging tools.

 $\label{processor} \mbox{\bf graphics} \ \mbox{get a picture of the processor net described by your $\sf CamlP3ls$ keleton expression to grasp the parallel structure of your program.$

parallel run your program in parallel over a network of workstations after a simple recompilation.

Presumably, you would run the parallel version once the program has satisfactorily passed the sequential debugging phase.

In the following sections, our running example is the computation of a Mandelbrot fractal set. We will describe the implementation program, compile it and run it in the three ways described above.

2.1 The Mandelbrot example program

The Mandelbrot example program performs the calculation of the Mandelbrot set at a given resolution in a given area of the graphic display. This is the actual program provided in the Examples directory of the distribution.

The computing engine of the program is the function pixel_row which computes the color of a row of pixels from the convergence of a sequence of complex numbers z_n defined by the initial term z_0 and the formula $z_{n+1} = z_n^2 + z_0$. More precisely, given a point p in the complex plane, we associate to p the sequence z_n when starting with $z_0 = p$. Now, we compute the integer m such that z_m is the first term of the sequence satisfying the following condition: either the sum of the real and imaginary parts of z_n exceeds a given threshold, or the number of iterations exceeds some fixed maximum resolution limit. Integer m defines the color of p.

p). This correspond to the following OCaml code:

```
open Graphics;;
let n = 300;; (* the size of the square screen windows in pixels
let res = 100;; (* the resolution: maximum number of iterations allowed *)
(* convert an integer in the range 0..res into a screen color *)
let color_of c res = Pervasives.truncate
      (((float c)/.(float res))*.(float Graphics.white));;
(* compute the color of a pixel by iterating z_m+1=z_m^2+c
(* j is the k-th row, initialized so that j.(i),k are the coordinates *)
(* of the pixel (i,k)
                                                                       *)
let pixel_row (j,k,res,n) =
 let zr = ref 0.0 in
 let zi = ref 0.0 in
  let cr = ref 0.0 in
 let ci = ref 0.0 in
 let zrs = ref 0.0 in
 let zis = ref 0.0 in
  let d = ref (2.0 /. ((float n) -. 1.0)) in
 let colored_row = Array.create n (Graphics.black) in
  for s = 0 to (n-1) do
    let j1 = ref (float j.(s)) in
    let k1 = ref (float k) in
    begin
     zr := !j1 *. !d -. 1.0;
     zi := !k1 *. !d -. 1.0;
      cr := !zr;
     ci := !zi;
     zrs := 0.0;
      zis := 0.0;
     for i=0 to (res-1) do
        begin
          if(not((!zrs +. !zis) > 4.0))
          then
            begin
             zrs := !zr *. !zr;
              zis := !zi *. !zi;
              zi := 2.0 *. !zr *. !zi +. !ci;
              zr := !zrs -. !zis +. !cr;
              Array.set colored_row s (color_of i res);
            end;
        end
      done
    end
  done;
```

```
(colored_row,k);;
```

In this code, the global complex interval sampled stays within (-1.0, -1.0) and (1.0, 1.0). In this 2-unit wide square, the pixel_row functions computes rows of pixels separated by the distance d. The pixel_row function takes four parameters: size, the number of pixels in a row; resolution, the resolution; k, the index of the row to be drawn; and, j, an array which will be filled with the integers representing the colors of pixels in the row. These values will be converted into real colors by the color_row function. In this program, the threshold is fixed to be 4.0. We name zr and zi the real and imaginary parts of z_i ; similarly, the real and imaginary parts of c are cr and ci; zrs and zis are temporary variables for the square of zr and zi; d is the distance between two rows.

The Mandelbrot computation over the whole set of points within (-1.0,-1.0) and (1.0,1.0) in the complex plane can be computed in parallel exploiting farm parallelism. The set of points is split by gen_rows into a bunch of pixel rows that build up the input stream, the computation of the Mandelbrot set on each row of complex points is independent and can be performed by the worker processes using pixel_row and the result is a stream of rows of pixel colors, each corresponding to an input pixel row.

```
(* draw a line on the screen using fast image functions *)
let show_a_result r =
 match r with
    (col,j) ->
      draw_image (make_image [| col |]) 0 j;;
(* generate the tasks *)
let gen_rows =
  let seed = ref 0 in
  let ini = Array.create n 0 in
 let iniv =
    for i=0 to (n-1) do
      Array.set ini i i
    done; ini in
  (function () ->
    if(!seed < n)
    then let r = (iniv,!seed,res,n) in (seed:=!seed+1;r)
    else raise End_of_file)
;;
```

The actual farm is defined by the mandel function which uses the parfun skeleton to transform a farm instance with 10 workers into an OCaml sequential function. Notice that the seq skeleton has been used to turn the pixel_row function into a stream process, which can be used to instantiate a skeleton. Finally the pardo skeleton takes care of opening/closing a display window on the end-node (the one running pardo), and of actually activating the farm invoking mandel. The function show_a_result actually displays a pixel row on the end-node. Notice that this code would need to be written anyway, maybe arranged in a different way, for a purely sequential implementation.

```
(* the skeleton expression to compute the image *)
let mandel = parfun (fun () -> farm(seq(pixel_row),10));;
```

2.2 Sequential execution

We assume the program being written in a file named mandel.ml. We compile the sequential version using camlp3lc as follows:

```
camlp3lc --sequential mandel
```

Remark 2.2.1 In the current implementation, this boils down to adding on top of mandel.ml the line

```
open Seqp31;;
```

to obtain a temporary file mandel.seq.ml which is then compiled via the regular Caml compiler ocamlc with the proper modules and libraries linked. Depending on the configuration of your system, this may look like the following

```
ocamlc -custom unix.cma graphics.cma seqp31.cmo
    -o mandel.seq mandel.seq.ml
    -cclib -lunix -cclib -lgraphics -cclib -L/usr/X11R6/lib
    -cclib -lX11
```

We highly recommend not to use explicit call to ocamle: use the camlp3lc compiler that is especially devoted to the compilation of CamlP3lprograms.

After the compilation, we get an executable file, mandel.seq, whose execution produces the picture shown on the left side of 2.1.

2.3 Graphical execution

It is often useful to look at the structure of the application process network, for example when tuning the performance of the final program. In CamlP3I, this can be done by compiling the program with the special option --graphical which automatically creates a picture displaying the 'logical' parallel program structure.

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```
camlp3lc --graphical mandel.ml
```

Figure 2.1: A snapshot of the execution of mandel.ml (left is sequential execution, right is parallel execution on 5 machines).

 $\mathbf{Remark}\ \mathbf{2.3.1}\ \textit{In the current implementation, this boils down to adding on top\ of\ \texttt{mandel.ml}}\ the\ line$

```
open Grafp31;;
```

to obtain a temporary file mandel.gra.ml which is then compiled via ocamlc with the proper modules and libraries. Depending on the configuration of your system, this may look like the following

```
ocamlc -custom graphics.cma grafp31.cmo -o mandel.gra mandel.gra.ml -cclib -lgraphics -cclib -L/usr/X11R6/lib -cclib -lX11
```

Once more, we highly recommend not to use explicit calls to ocamlc: use the camlp3lc compiler that is especially devoted to the compilation of CamlP3lprograms. \diamond

After compilation, we get the executable file mandel.gra, whose execution produces the following picture.

2.4 Parallel execution

Once we have checked the sequential version of our code, and got a picture of the structure of the parallel network, we are ready to speed up the computation by using a network of computers.

2.4.1 Compilation for parallel execution

We call the compiler with the special option **--parallel** devoted to compilation for parallel execution:

```
camlp31c --parallel mandel
```

Remark 2.4.1 In the current implementation this boils down to adding on top of mandel.ml the lines

```
open Parp31;;
open Nodecode;;
open Template;;
```

to obtain a temporary file mandel.par.ml which is then compiled via ocamlc with the proper modules and libraries. Depending on the configuration of your system, this may look like the following

```
ocamlc -custom unix.cma p3lpar.cma -o mandel.par mandel.par.ml -cclib -lunix -cclib -lgraphics -cclib -L/usr/X11R6/lib -cclib -lX11
```

Once again, we highly recommend not to use explicit calls to ocamlc: use the camlp3lc compiler that is especially devoted to the compilation of CamlP3lprograms.

The compilation produces an executable file named mandel.par.

2.5 Common options

The parallel compilation of CamlP3I programs creates executables that are equipped with the following set of predefined options:

- -p3lroot, to declare this invocation of the program as the root node.
- -dynport, to force this node to use a dynamic port number instead of the default p3lport; in addition the option outputs it (useful if you want to run more slave copies on the same machine).
- -debug, to enable debugging for this node at level n. Currently all levels are equal.
- -ip, to force the usage of a specified ip address. Useful when you are on a laptop named localhost and you want to be able to choose among network interfaces.
- -strict, to specify a strict mapping between physical and virtual processors.
- -version, to print version information.
- -help or --help Displays this list of options.

2.5.1 Parallel computation overview

The executable produced by using the **--parallel** option of the compiler behaves either as a generic computation node, or as the unique *root configuration node*, according to the set of arguments provided at launch time.

To set up and launch the parallel computation network, we need to run multiple invocations of the parallel executable:

- run one copy instance of mandel.par, with no arguments, on each machine that takes part to the parallel computation; These processes wait for configuration information sent by the designated *root node*,
- create a root node, by launching one extra copy of mandel.par with the special option -p3lroot.

As soon as created, the root node configures all other participating nodes and then executes locally the pardo encapsulated sequential code.

In addition to the **-p31root** special option, the root node invocation must specify the information concerning the machines involved in the computational network (their ip address or name, their port and color).

2.6 Launching the parallel computation

Here is a simple script to launch the parallel network on several machines:

```
#!/bin/sh
# The list of machines
NODES="machine1 machine2 machine3 machine4"
# The name of executable to be launched
PAR="./mandel.par"
echo -n "Launching CamlP31 $PAR on the cluster:"
for NODE in $NODES; do
                         #(*1*)
    echo -n " $NODE"
#launching a generic computation node on each machine
    ssh $NODE $PAR 1> log-$NODE 2> err-$NODE &
# a possible coloring of machines
    case $NODE in
                                                     #(*2*)
        machine1) COLORED_NODES="$COLOREDNODES $NODE#1";;
        *) COLORED_NODES="$COLOREDNODES $NODE#2";;
    esac
done
echo "Starting computation with $COUNT node(s): $COLORED_NODES..."
# launch the unique root configuration node #(*3*)
$PAR -p3lroot $COLOREDNODES 1> log-root 2> err-root
echo "Finished."
```

This script assumes mandel.par to be accessible to all participating machines and does the following:

- runs mandel.par on all participating machines (#(*1*)),
- generates a coloring for participating nodes (#(*2*)),
- launches the computation starting the root process on the local machine (#(*3*)) providing the list of colored participating hosts.

In future versions, especially those incorporating the MPI communication layer, the startup mechanism will possibly work differently (typically, the initialization steps will be performed by the MPI layer).

2.7 Common errors

A few words of warning now: even if the user program is now easy to write, compile and execute, you should not forget that the underlying machinery is quite sophisticated, and that in some situations you may not get what you expected. Two typical problems you may encounter are the following:

output value: code mismatch If you see this error in the parallel execution of your program, it means that two incompatible versions of your program are trying to communicate. OCaml uses an MD5 check of the code area before sending closures over a channel, because this operation only makes sense between "identical" programs.

Two possible reasons for the error are:

- an old version of your program is still running somewhere and is trying to communicate with the newer version you are running now. You should kill all the running processes and try again.
- you are running copies of the program compiled for different architectures. This
 feature is not yet supported, and you should run the program on homogeneous
 architectures.

references You should remember that the user functions provided to the skeletons will be all executed on different machines, so their behaviour *must not* rely on the existence of implicitly shared data, like global references: if you do, the sequential behaviour and the parallel one will be different. This does not imply that all user function be real functions (you can use local store to keep a counter for example), but an access to a global reference is certainly a mistake (since every node will access its *own private* copy of the data, thus defeating the purpose of the shared data).

Chapter 3

More programming examples

3.1 Generating and consuming streams

Streams to be feed to the parallel networks can be created and consumed using functions in P31stream. Main functions are as follows:

Function	Description	Secs
P3lstream.of_list	transforms a list in a valid stream	3.1.1, 3.1.2,
		3.5
P31stream.iter	iterates on all elements of a stream	3.1.1, 3.1.2,
		3.1.3
P31stream.of_fun	allows stream generation	
	iterating a sequential function	
	which explicitely raises End_Of_File	3.1.3
P3lstream.to_list	transforms streams into lists	3.1.4

3.1.1 Generating streams from lists

```
let rec generate_list_of_float n s =
   if ( n <= 0 ) then []
   else s :: (generate_list_of_float (n-1) (s +. 1.0))
;;
let initseq n s = P3lstream.of_list (generate_list_of_float n s);;
let finseq y =
   P3lstream.iter (fun x -> print_float x; print_newline()) y;;

(* Define stage1 and stage 2, can be anything.....*)
let stage1 _ x = x +. x;;
let stage2 _ x = x *. x;;

(* definizione network del pipe *)
let pipe = parfun (fun () -> seq(stage1) ||| seq(stage2));;
```

```
(* pardo activation *)
pardo
  (fun () ->
    let    s = initseq 10 1.0 in
    let    y = pipe    s in
        finseq y
);;
```

3.1.2 Generating streams from files

```
let read_input_float fd =
  Scanf.fscanf fd "%f" (fun n -> n);;
let rec fgenerate_list_of_float cin n=
    if ( n <= 0 ) then []
    else
      (try
 (let s = (read_input_float cin) in
            Printf.printf "Ecco %f\n" s;
    s:: (fgenerate_list_of_float cin (n-1)))
   End_of_file -> [];
     )
;;
(* stream generation *)
let initseq cin n =
      P3lstream.of_list (fgenerate_list_of_float cin n);;
(* prints out stream *)
let finseq cout y =
  P3lstream.iter (fun x -> Printf.fprintf cout "%f" x; output_string cout "\n") y;;
(* Defines stage1 and stage 2 *)
let stage1 _{x} = x + . x;;
let stage2 _{x} = x *. x;;
(* defining a two stage pipe network *)
let pipe = parfun (fun () -> seq(stage1) ||| seq(stage2));;
(* pardo activation *)
pardo
     let cin = open_in "pippo" and cout = open_out "pluto" in
     let s = initseq cin 10 in
     let y = pipe s in
      finseq cout y
```

```
)
;;
```

3.1.3 Generating streams repeatedly calling a function

Here, the stream is generated by repeatedly calling function <code>generate_input_stream</code> via <code>P3lstream.of_fun</code>.

```
%quinto-esempioUM.ml
(* generating the input stream calling repetedly a function *)
let generate_input_stream =
  let x = ref 0.0 in
  (function () ->
    begin
      x := !x + . 1.0;
      if(!x < 10.0) then !x else raise End_of_file</pre>
    end);;
(* prints out an integer stream *)
let finseq y =
 P3lstream.iter (fun x -> print_float x; print_newline()) y;;
(* Defines stage1 and stage 2 as identity*)
let stage1 _ x = x;;
let stage2 _{x} = x;
let pipe = parfun (fun () -> seq(stage1) ||| seq(stage2));;
(* pardo activation *)
pardo
     let s = P3lstream.of_fun generate_input_stream in
     let y = pipe s in
       finseq y
  )
;;
        Transforming streams into lists
(* generating the input stream calling repeatedly a function *)
let generate_input_stream =
  let x = ref 0.0 in
  (function () ->
   begin
      x := !x + . 1.0;
      if(!x < 10.0) then !x else raise End_of_file</pre>
    end);;
(* Defines stage1 and stage 2*)
```

3.2 Global and local definitions

As discussed in Section 2.7, global variables *must* not be used in an CamIP3I pragram, as their value on different processing nodes will be different and updates will have effect only on the node which executes them.

On the other hand, we can have both local and global definitions which are evaluated before or after specializing a processing node. For instance we can share the same file descriptor between all the processing nodes partecipating to a skeleton. See examples in Section 1.3.3.

3.3 Managing command line: option

To be done

3.4 Directing allocation: colors

To be done

3.5 Mixing Unix processes with CamlP3

The following code defines a farm in which each worker computes the square over a stream of float. However, the function is computed by an external command which is spawned and connected via stdin / stdout to the farm worker in the seq skeleton. In the following code, care is taken to activate the external process only once. spawned is true only if the Unix process and connecting pipes descriptor are maintained in variables cin and cout. Notice that pattern matching in (* * *) is not exhaustive, because if process has been already spawned cin and cout must contain a valid descriptor.

```
let farm_worker _ =
  let conto = ref 0 and spawned = ref false
```

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```
and cin = ref None
  and cout = ref None in
    (fun x \rightarrow
       conto := !conto + 1;
       if not !spawned then
begin
   let (ic,oc) = Unix.open_process "./square"
   in cin := Some ic; cout := Some oc; spawned:=true
       let Some ic, Some oc = (!cin , !cout) in (* * *)
Printf.fprintf oc "%d\n" x; Pervasives.flush oc;
let i = Scanf.fscanf ic "%d" (fun x -> x) in
    )
;;
let compute = parfun (fun () -> farm(seq(farm_worker),4));;
let print_result x = print_int x; print_newline();;
pardo(fun () ->
let is = P3lstream.of_list [1;2;3;4;5;6;7;8;9] in
let s' = compute is in P3lstream.iter print_result s';
    );;
   The important thing is remember to fflush data output in the external commend source
otherwise we block. The following is an example of valid C definition for the square
program.
#include <stdio.h>
#define TRUE 1
int main(void)
  int i;
  while (TRUE) {
      /* reading from standard input */
      scanf("%d",&i);
      /* writing on strandard output */
      printf("%d\n",i*i);
      /* fflushing buffers otherwise you block the output stream */
      fflush(NULL);
 }
  exit(0);
```

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Chapter 4

Implementing CamIP3I

Now, let us point out the peculiar features relative to the implementation of CamlP3l. First, we will discuss the mechanism used to implement different processes onto different nodes, by exploiting a particular form of "closure communication". Then, we will point out some details relative to the interprocess communication layer and we will motivate the choice of the Unix sockets as the CamlP3l communication layer. Finally, we will discuss some details of the templates we used to implement the skeletons provided by CamlP3l.

4.1 Closure passing as distributed higher order parameterization

A sequential implementation of an CamlP3l program is quite easy to provide: just use a library seqp31.ml which implements each skelton with a valid OCaml sequential function. The type safety is a direct consequence of the fact that we are not using here anything from outside the safe core of Ocaml.

Similarly, providing the graphical semantics poses no real challenge.

But what about the parallel semantics? What is the right way to implement such a thing? We must guarantee the type safety and ensure that the runtime is reasonably small as to allow the verification of its properties, which will become an important point in industrial applications. Both points posed problems which we overcame during the development of the system.

First of all, to ensure that the system is manageable and safe, we immediately discarded the approach based on parsing the source file to extract the code corresponding to each node of the network: this would impose to use external tools to perform an analysis of the user code which is difficult, error prone, and whose semantics would have a very unclear status.

Instead, we choose to use an SPMD approach: all the nodes of the network will run the *same* program (in a sense this is the "template process interpreter code", as we will see in while), which will be the result of the compilation of the full user code, and a control node will dispatch to the rest of the nodes in the network the parameterization information needed to specialize it to the particular function it is really supposed to perform (emitter, collector, sequential node running a given function f, etc.).

 $^{^1{}m The}$ control node runs the same program as the others, but it is invoked by the user with a special designating option <code>-p31root</code>.

In order to achieve this behavior, the control node performs the following tasks:

- executes the parfun skeleton expression definitions, which has as a consequence to build a data structure describing all the parallel process networks. From this data structure, we compute behind the scenes the configuration information for each node in the process network.
- executes the pardo expression: this has the following effect
 - maps virtual nodes to the processor pool given on the command line,
 - initializes a socket connection with all the participating nodes,
 - gets the port addresses from each of them (a fixed port number —p31port or some dynamically generated number if more than one copy run on the same machine),
 - sends out to each node the addresses of its connected neighbors (this step together with the previous two provides an implementation of a centralized deadlock free algorithm to interconnect the other nodes into the process network specified by the skeleton expression),
 - sends out to each node the specialization information that consists of the function it must perform.

This very last task requires a sophisticated operation: sending a function (or a closure) over a communication channel. This is usually not possible in traditional functional programming languages, since sending an arbitrary function supposes that we are able to find on the receiving side the code corresponding to the function name received or that we can transfer executable code (a feature known as mobility today). Now, mobility is necessary to send closures between arbitrary programs (since two different programs have no reason to know each other's function code), but not between two copies of the same program: in the latter case, it suffices to send what essentially amounts to a code pointer. Starting from version 1.06, OCaml contains a modified marshaling library, originary designed for the CamlP3l system, that performs closure sending between copies of the same program (this is checked by means of an MD5 signature of the program code). The ocaml run time system takes care of dealing with differences in endianness and word size between communicating machines, as well as flattening tree-shaped data structures.

On the other side, all the other nodes simply wait for a connection to come in from the root node, then send out the address of the port they allocate to do further communication, wait for the list of neighbors and for the specialization function, then simply perform it until termination.

To summarize, in the implementation the possibility of sending closures allowed us to obtain a kind of higher order distributed parameterization that kept the runtime code to a minimum size (the source codes of the full system is less than twenty kilobytes).

4.2 Communication and process support

As far as the general mechanism of closure passing is concerned, no particular requirement/restrictions have been posed onto the physical communication implementation. Even considering the fact that we need to move data between the different processes making up the parallel implementation of an CamlP3I program, we derived no particular constraint onto the communication layer. Thus, at the very beginning of the CamlP3I project, we faced the problem of choosing a suitable communication system. We had as a goal to come out with the maximum "portability" of CamlP3I. Furthermore, we wanted to fully demonstrate the feasibility of integrating the parallel skeleton world within a functional framework. These two goals had priority over the classical "efficiency and performance" goal one usually has to achieve when dealing with parallelism.

The result is that we have adopted the plain Unix socket world as the communication layer. This has some (very) positive consequences on the overall CamIP3I design:

- the socket communication support is generally available on Unix/Linux and Windows system
- no particular customization of the support is needed to match the CamIP3I features,
- the point-to-point, connection oriented, stream model provided by Unix sockets is
 perfect to model data streams flowing around between the processes belonging to
 the process network derived by CamlP3I to implement the user skeleton code,
- last but not least, there was an existing and suitable ocaml interface to Unix system calls, including those relative to sockets.

On the down side, the adoption of Unix sockets presents an evident disadvantage which is the low performance achieved in communications (a raw synchronization (i.e. zero length data communication) takes several milliseconds to be performed, even in those cases when the data transmission media turns out to be free, i.e. no collisions are detected).

At the moment, we are considering to use in the next version of CamlP3I a communication layer based on an optimized communication library such as MPI [18], as an efficient alternative to the socket communication layer, which will be nevertheless retained for its ease of deployment, that makes it attractive for programming courses.

Porting to MPI will require some modifications in the template code used within CamlP3I, and will not necessarily completely solve the performance problems of the socket communication layer when run on a network of computers, where most MPI libraries are still implemented using sockets, but will allow to target real multiprocessor machines where MPI is efficiently implemented, without touching the user code. Also, we will be able to delegate to the MPI system the administrative tasks involved in copying and launching the programs on the different machines.

As far as the process model is concerned, we felt happy with the Unix one. All we need is a mechanism allowing an instance of the template interpreter (the one specialized by using the closure passing mechanism) to be run onto different workstations belonging to a local area network. The Unix rsh mechanism matches this requirement. Note that, as processes are generated and run on different machines just at the beginning of the CamlP3I program execution, any considerations about performance in rsh-ing is irrelevant.

4.3 Template implementation

CamlP3I implements each skeleton appearing in the application code by generating a proper instantiation of the corresponding implementation template. In CamlP3I, a single implementation template is provided for each one of the skeletons supported. The implementation templates provided within the current prototype closely resemble the ones discussed in the informal parallel semantics section (Section 1.3). Actually, only the *reduce* template is slightly different, in that the tree discussed in Section 1.3.7 is actually implemented by a process network similar to the one discussed for the farm, where partially evaluated

data is iteratively passed back from the collector to the emitter process. We are currently studying a more efficient mechanism based on a formal calculus for data distribution and computation over dense arrays [17, 8, 7].

Each template appearing in CamIP3I:

- is parametric in the parallelism degree exploited As an example the farm template may accommodate any positive numbers of worker processes. Currently, the programmer must specify this parameter, which is the second parameter of a farm(f,n) skeleton call.
- is parametric in the function computed as the body of the skeleton For instance, the farm skeleton accepts as a parameter the function that has to be computed by the worker processes. This function must be a skeleton itself. Therefore, either it is a seq skeleton call, or it is a skeleton call modeling a parallel computation. In the former case, the skeleton is implemented by a process network whose workers just perform the sequential computation f denoted by some seq(f). In the latter case, each worker process is itself a process network known by the emitter and collector processes implementing the farm just as channels where data has to be delivered/fetched.
- provides a set of process templates i.e. parametric process specifications that can be instantiated to get the real process codes building out the implementation template process network. As an example, consider again the farm template. The emitter process behavior can be fully specified by the data type of items that have to be processed, by the channel from which those data items have to be read and by the set of channels onto which the data items have to be scheduled (written) to the worker processes, possibly with some "clever" (e.g. achieving load balancing) scheduling strategy. Such a process can be completely specified by providing a function

```
farmetempl (OutChanSel f) ic ocl
```

whose first parameter provides the worker scheduling function, the second one provides the input channel where data has to be fetched and the third one provides the set of channels used to deliver tasks to be computed to the farm workers. The type of such a function turns out to be

The process template definition in the CamIP3I code looks like the following:

```
let farmetempl (OutChanSel f) ic ocl =
  while true do
    try
    let theoc = f ocl in
    match (Marshal.from_channel ic) with
      UserPacket(p,seqn,tl) ->
         Marshal.to_channel
         theoc
         (UserPacket (p,seqn,Farmtag::tl))
         [Marshal.Closures];
      flush theoc;
         | EndStream ->
          List.iter
```

Therefore the whole compilation process transforming an CamlP3I skeleton program into the parallel process network implementing the program can be summarized in the following steps:

- 1. the skeleton code is parsed and transformed into a skeleton tree data structure, recording all the significant details of the skeleton nesting supplied by the user code,
- 2. the skeleton tree is traversed and processes are assigned to each skeleton according to the implementation templates. During this phase, processes are denoted by their input/output channels, identified via a unique number.
- 3. once the number and the kind of parallel processes building out the skeleton code implementation is known, code is generated that either delivers the proper closures, derived by using the process templates, to the "template interpreter" instances running on distinct workstations (this happens just on one node, the "root" one), or waits for a closure and repeatedly computes this closure on the proper input and output channels until an EndOfFile mark is received.

Chapter 5

Multivariant semantics and logical debugging

By providing modules that implement the three CamIP3I skeleton semantics (the sequential one, the parallel one and the graphical one), we allow the CamIP3I user to perform the following parallel application development process:

- develop skeleton code modeling the application at hand. This just requires a full understanding of the skeleton sequential semantics and usually allows the user to reuse consistent portions of existing applications written in plain ocaml or legacy in C, C++ etc.
- test the functionality of the new application by supplying relevant input data items
 and looking at the results computed using the sequential skeleton semantics. In case
 of problems, the user may run the sequential debugging tools to overcome problems.
- link the parallel skeleton semantics module and run the application onto the workstation network. Provided that the application was sequentially correct, no new errors should be found at this step (we assume that the run time is guaranteed correct!). In practice, a few errors can occur usually related to wrong assumption on global variables. If your code uses global variables updating them durin gexecution, this will work OK in the sequential semantics as memory is actually shared but not in the parallel version as update will be only seen locally on the processing node.
- look at the performance results of running the application on the number of processors available and possibly adjust the significant performance parameters, such as the number of workers of the farm, map and reduce and the color of each of them. This is actually the real problem in the development of an efficient parallel application. Forthcoming versions of CamlP3I will include analytical performance models for the templates and these models will be used to automatically guess colors and giude the complier in the compiler. During performance tuning, the programmer may link the graphic semantic skeleton module and look at the results of the program execution, i.e. at the resulting process graph, in order to understand where bottlenecks are or which parts of the program must be further decomposed using skeletons in order to get better performant application code.

Let us spend now some words concerning logical, sequential debugging of $\mathsf{CamIP3I}$ applications.

A user developing an CamlP3I application may link the sequential skeleton semantics module to his/her code and debug the application by using the plain sequential debugging tools of ocaml. This debugging activity can be performed on a single machine, provided the machine supplies ocaml. Also, performance tuning can be directed using standard sequential profiling tools such as gprof.

Once the application has been debugged, i.e. the user perceives it computes the expected results, he/she can compile the parallel version of the application by linking the parallel skeleton semantics. As we guarantee that the implementation templates for the different skeletons of CamlP3I are correct (deadlock free, load-balanced, etc.) and as we guarantee that the process transforming the skeleton code in the process code is correct, the user does not need to perform explicit activities in order to check that the results computed by the parallel code are correct.

In particular, the user does not need to check that all the processes have been correctly scheduled for execution, or that the communication channels have been set up properly between these processes, or that data of type 'a has been never delivered on channels transmitting data of type 'b. This is a very short list of bad things that may affect the correct behavior of an explicitly parallel program, indeed. The fact that the user is not required at all to take them into account is one of the biggest pro's of the functional skeleton approach.

Chapter 6

Related work, conclusions and perspectives

6.1 Related work

Many researchers are currently working on skeletons and most of them are building some kind of parallel implementation, but our work, as far as we know, is unique in its combination of a fully functional strongly typed language with the skeleton approach.

In particular, Darlington's group at Imperial College in London is actively working on skeletons. They have explored the problems relative to implementing a skeleton programming system, but the approach taken uses an imperative language as the implementation language. Currently there is a "local" prototype implementation but no public domain implementation of their skeleton approach and they seem deeply involved in the study of the data-parallel and coordination aspects of skeletons. [13, 12, 1]

A different approach relative to skeleton parallel programming within a functional framework has been discussed by Bratvold [4]. Bratvold takes into account plain ML programs and looks for skeletons within them, compiling these skeletons by using process networks that look like implementation templates. However, both the final target language and the implementation language are imperative.

Finally, Sérot [23, 22], presents an embedding of skeletons within ocaml that seems to be close to our work, although independently developed. The message passing is performed by interfacing the MPI library with ocaml. The skeletons taken into account are different. She considers data-parallel farm, roughly corresponding to our mapvector skeleton, and two further skeletons, scm and filt. filt is a plain filter skeleton, canceling data items from a list, while scm (Split, Compute and Merge) looks like a map skeleton working on lists with explicit, user defined, decomposition/recomposition functions.

Sérot's implementation of the skeletons within ocaml is quite different from ours and only allows one skeleton at a time to be realized on the processor networks, thus preventing skeleton composition (you cannot nest two scm skeletons for example), and only allowing for a limited form of staging of the parallel computation: you can perform an scm, then when this is finished, you can reorganize your network and perform another scm. This way, the mapping of virtual processors to real processors on the network is a trivial task, and is done inside each skeleton at run-time instead of beforehand in a specific pass like in CamlP3I. Sérot implements the skeletons included in his model by providing second order

functions that directly call MPI and realize an SPMD execution model.

As for the relevant effort done in the field of languages for mobile agents, like for example [16, 15], it should be noted that they address quite a different kind of problems, but once stable, these languages could form the basis of a next generation fully fault-tolerant and dynamically load-balanced version of our system.

6.2 Conclusions and perspectives

Here we showed how a skeleton parallel programming modelcan be successfully married with the functional programming environments such as the one provided by OCaml.

In particular, we discussed a powerful skeletal model, how skeletons can be embedded within OCaml as second order functions and how modules implementing both the sequential and the parallel skeleton and discuss the typical application development cycle in CamlP3I. The whole process preserves the strong typing properties of ocaml.

At the moment, the prototype CamlP3I implementation is being tested as described in this paper and is available from the CamlP3I project home Web page

http://camlp31.inria.fr/.

In the near future we want first of all to include a more powerful MAP skeleton working on dense arrays with an arbitrary number of dimensions[17, 8, 7]. This will call for a more efficient communication layer, by using colective MPI communications [18] instead of the plainUnix socket library. At the same time, we investigate the feasibility of porting the system on the ubiquitous Windows boxes, for didactical purposes. Finally, we already developed a parallel numerical code [5] and plan to write some more significant parallel applications in order to fully test the prototype.

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